

## Results: Time-Invariant Single Path Channels

### Assumptions and Simulation Parameters:

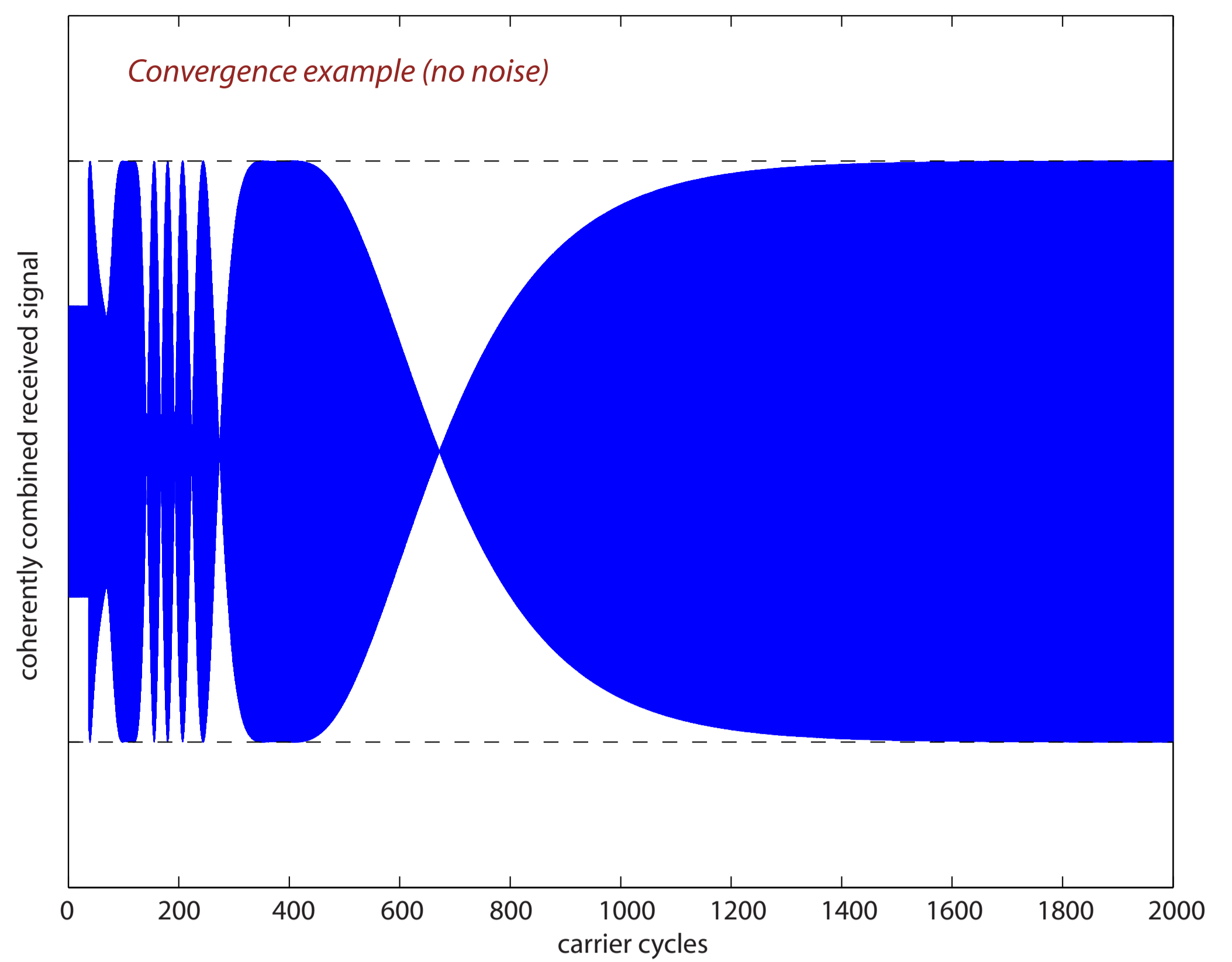
- Single-path, unit-gain channels  $g_{ij} = g_{ji} = \delta(t - \tau_{ij})$ .
- Randomly generated time-invariant channel propagation delays.
- Randomly generated initial VCO phases.
- Primary beacon frequency  $\omega_0 = 2\pi \cdot 800 \cdot 10^6$  rad/sec.
- Unmodulated unit-amplitude carriers at  $\omega_c = 2\pi \cdot 3.2 \cdot 10^9$  rad/sec.

### FS-PLL parameters:

- Three-state phase-frequency detectors with slope  $K_d = 1$  V/rad.
- VCO sensitivity  $K_0 = 2\pi \cdot 10^5$  rad/s.V.
- FS-PLL dividers set to  $M_1 = M_2 = 1$  and  $N_1 = N_2 = 2$ .
- Analog loop filter transfer function

$$F(s) = \frac{RC_2s + 1}{RC_1C_2s^2 + C_2s}$$

Each loop filter's bandwidth is set to 10 MHz to facilitate rapid convergence to locked state.



## Results: Time-Varying Single Path Channels

### Assumptions and Simulation Parameters:

- Single-path, unit-gain channels  $g_{ij} = g_{ji} = \delta(t - \tau_{ij}(t))$ .
- Piecewise-constant source/destination acceleration model (0.5 second intervals, uniformly distributed on  $[-10,10]$  m/s<sup>2</sup>).
- Randomly initialized time-varying propagation delays.

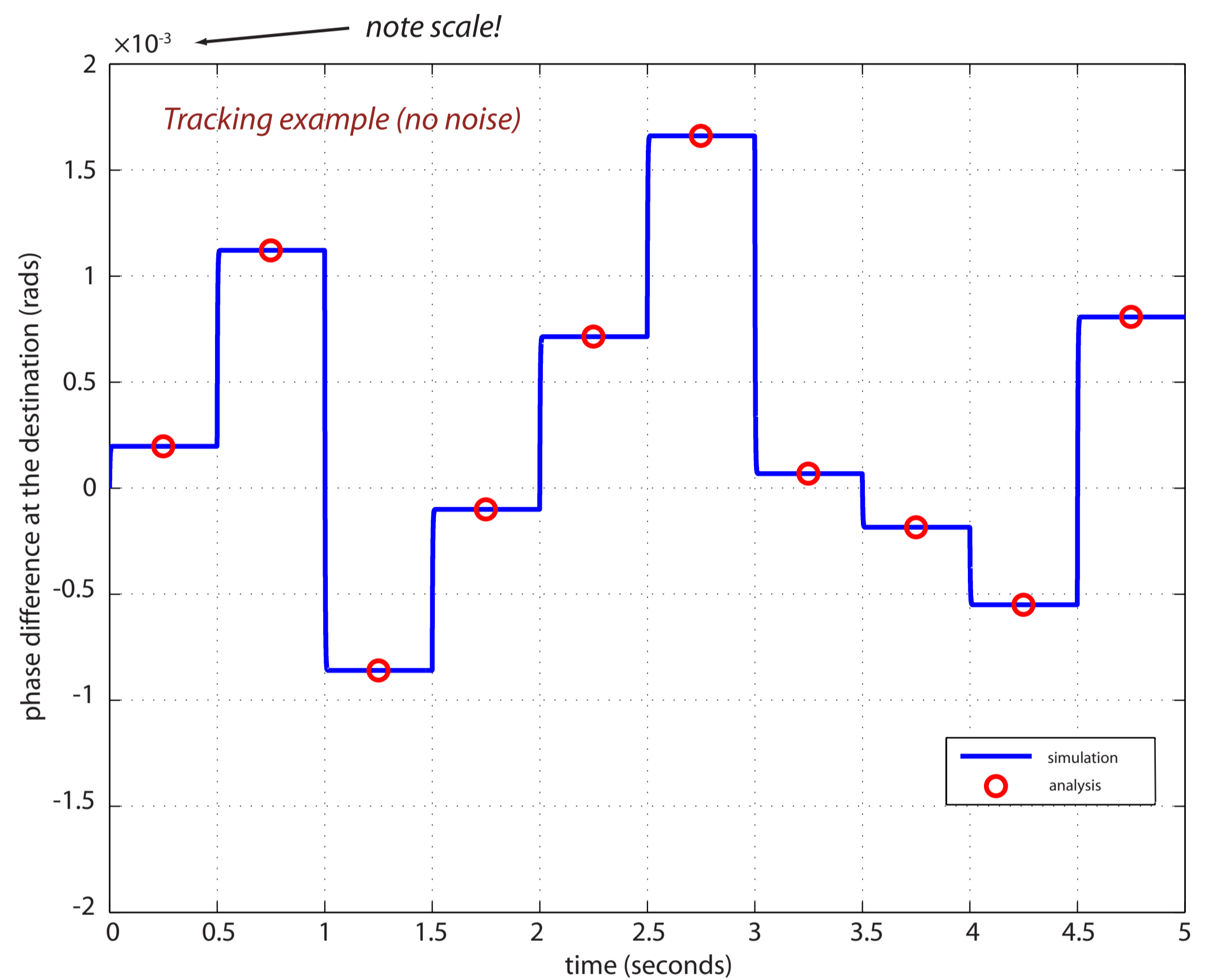
### FS-PLL parameters:

- All same as before except 500 Hz PLL loop filter bandwidth.

Each PLL must track a linear frequency ramp. Tracking errors will result in phase offset at the destination. Analysis of PLL steady-state phase error shows that the phase offset at destination is

$$\phi_{\Delta} = (N_1\kappa_1 + N_2\kappa_2)(\alpha_{01} - \alpha_{02})\frac{\omega_c}{c}$$

where  $\kappa_i$  is inversely proportional to the square of the closed loop bandwidth of the PLLs and  $\alpha_{0i}$  is the constant acceleration in the path between source  $i$  and the destination. The analysis assumes that the PLL remains in the locked state.



## Results: Time-Varying Multipath Channels

To understand how the synchronization performance degrades from single-path to general multipath, we consider a Ricean channel model with Rice factor  $K$ . The phase of the Ricean channel can be written as

$$\theta = \theta_{LOS} + \Theta \quad \leftarrow \text{Random component}$$

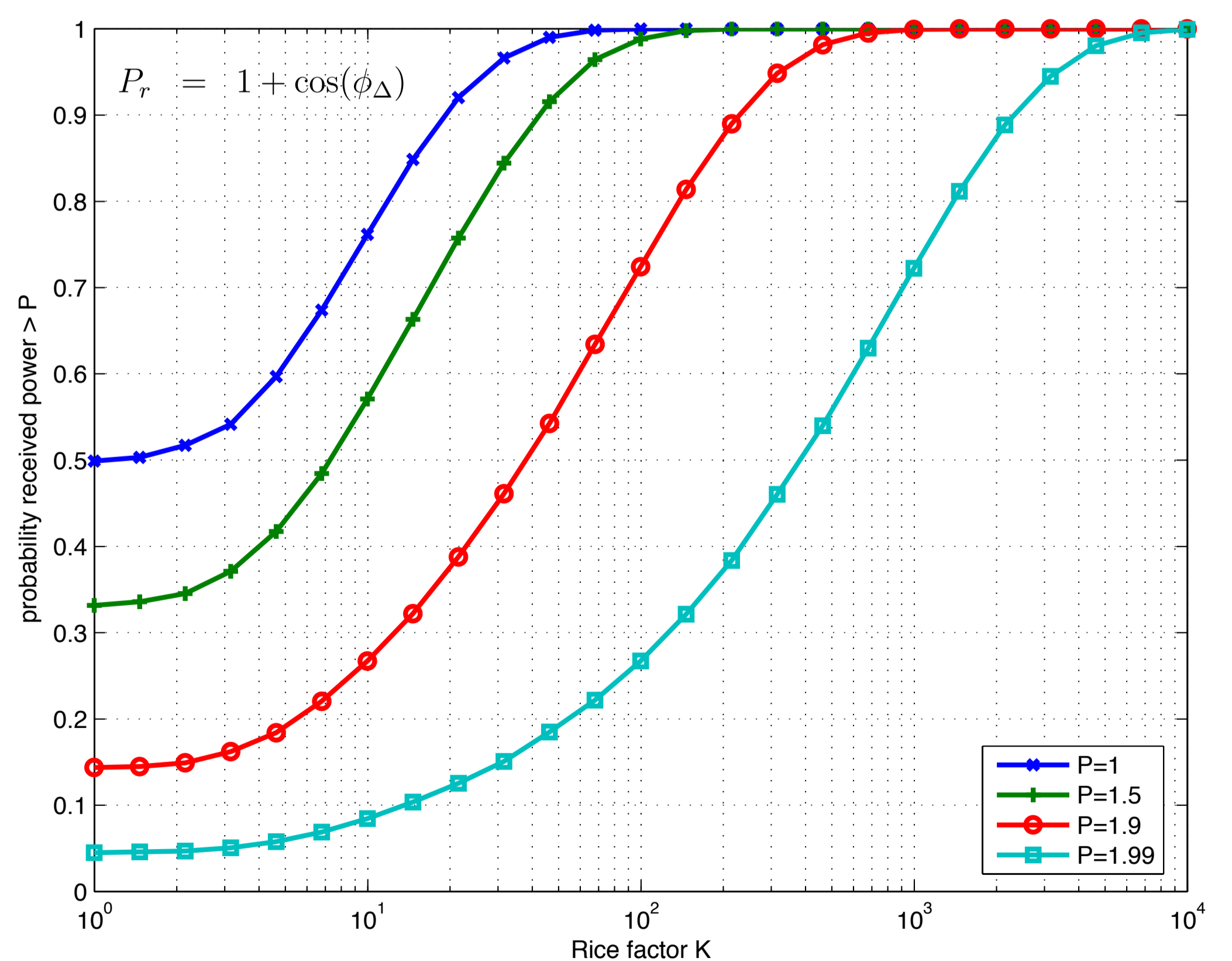
The random carrier phase offset at the destination can be written as

$$\phi_{\Delta} = \frac{N_1N_2}{M_1M_2}\Theta_{01} - \Theta_{10} + \frac{N_1N_2}{M_1M_2}\Theta_{02} - \Theta_{20}$$

where  $\Theta_{0i}$  is the phase perturbation at  $\omega_0$  and  $\Theta_{i0}$  is the phase perturbation at  $\omega_c$ . Distribution for  $\Theta$  given in the paper.

### Assumptions and Simulation Parameters:

- Unit-gain Ricean channels (to isolate the effect of phase offsets).
- Each channel's has the same Rice factor  $K$ .
- Line-of-sight component is identical in both directions.
- Time-variations of the channel are sufficiently slow such that any PLL phase tracking error is negligible.



## Conclusions:

- » Explicit method proposed for two-source carrier phase and frequency synchronization.
- » Evaluated in three channel models.
- » Method allows for high levels of source/destination mobility.
- » Explicit description of performance degradation to general multipath channels.
- » Paper provides more details and discusses practical considerations.

